

امتحان دور يناير ٢٠١١ المستوى : الثالث شعب: برامج * التاريخ: ٢٠١١ / ١ / ١٧ الزمن: ساعتان		جامعة المنصورة كلية العلوم -- قسم الرياضيات المادة: إحصاء حيوي كود المادة : ر ٣٠١ الدرجة الكلية : ٨٠ درجة
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Answer the following questions

Q1: (25 marks)

A random sample of size 36 is taken from a population with mean μ and variance σ^2 and tabled as :

Classes	2 — 4	4 — 6	6 — 8	8 — 10	10 — 12
frequency	6	7	10	7	6

(a) Find the median (M), the mode (D) and standard deviation (S) **(15 marks)**

(b) Compute a 95 % confidence interval for the mean μ . **(10 marks)**

Q2: (25 marks)

(a) Let X be a random variable has density function $f(x) = \begin{cases} ae^{-3x} & : x \geq 0 \text{ and } a > 0 \\ 0 & \text{otherwise} \end{cases}$

Find (i) The value of a (ii) $p(X = 3)$ and $p(X < 3)$ (iii) $E(X)$ and $V(X)$.

(b) A fair coin is tossed 10 times. Let X be the number of heads which appear .

Find $p(X = 4)$ and $p(X < 4)$. **(10 marks)**

Q3: (30 marks)

(a) Let X be a random variable having values 1 , 3 , 5 , 7 , 9 , 11 and Y another random variable having values 2 , 4 , 6 , 8 , 10 , 12 . Compare between the dispersion of the values X and the dispersion of the values Y. **(10 marks)**

(b) A random sample of size 49 is taken from a normal population with mean 12 and variance 36 . Find $p(\bar{X} \geq 14)$. **(10 marks)**

(c) A random sample has elements 8.5 , 11.5 , 9.5 , 10.5 , 8 , 9 , 11 , 10 , 12 is taken from a normal population $N(\mu, \sigma^2)$ with unknown mean and unknown variance. Find 95% confidence interval for μ . **(10 marks)**

Note that : $p(Z < 2.34) = 0.99$ $p(Z > 2.34) = 0.01$ $p(Z < 1.5) = 0.93$

$Z_{0.025} = 1.96$, $Z_{0.05} = 2.58$ $t_{(0.025, 8)} = 2.3$, $t_{(0.05, 8)} = 3.35$ $t_{(0.025, 9)} = 2.26$