



أجب عن الأسئلة الآتية :-

السؤال الأول: (أ) أخذت عينة عشوائية مكونة من 400 فرد من إحدى المدن فوجد أن المدخنين منهم 100 فرد . أوجد
95 % فترة ثقة لنسبة المدخنين بتلك المدينة . (10 درجات)

(ب) لمعرفة تأثير دواء على قراءات ضغط الدم المرتفع. أخذت لذلك عينة عشوائية مكونة من 9 أشخاص و قيس ضغط
كل منهم قبل تعاطي ذلك الدواء و بعد تعاطيه لمدة أسبوع فكانت النتائج كالتالي :

| | | | | | | | | | |
|--------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| القراءة قبل تعاطي الدواء | 170 | 180 | 160 | 175 | 150 | 180 | 185 | 190 | 195 |
| القراءة بعد تعاطي الدواء | 163 | 168 | 149 | 163 | 142 | 168 | 177 | 179 | 186 |

احسب 95 % فترة ثقة لمتوسط الانخفاض في قراءة ضغط الدم الذي ينتج من استخدام هذا الدواء (15 درجة)

السؤال الثاني: (أ) إذا كان الوسط الحسابي للتوزيع الطبيعي μ معلوم . أثبت أن المقدر $S^2 = \frac{1}{n} \sum_{i=1}^n (X_i - \mu)^2$

مقدر كاف لتباين التوزيع الطبيعي σ^2 (10 درجات)

(ب) إذا كانت أعمار المصابيح الكهربائية X (بالسنين) التي تنتجها احدي الشركات يتبع توزيعاً احتمالياً دالة كثافته
الاحتمالية هي $f(x) = 12x^2(1-x)$; $0 \leq x \leq 1$ إذا أخذنا عينة عشوائية مكونة من 64 مصباح فما

احتمال أن يكون متوسط أعمارها أقل من $7\frac{1}{2}$ شهر (15 درجة)

السؤال الثالث: (أ) إذا كانت X_1, X_2, \dots, X_n عينة عشوائية من المشاهدات المستقلة المسحوبة من توزيع

بواسون بمعلم λ . أثبت أن : $I_{SA}(\lambda) = \frac{n}{\lambda}$ (10 درجات)

(ب) احسب حجم العينة اللازم سحبها من مجتمع حجمه 20000 لتقدير المتوسط لظاهرة معينة بخطأ لا يتعدى 2

بدرجة ثقة 99 % بفرض أن تباين تلك الظاهرة في المجتمع 16 (10 درجات)

(ج) أوجد مقدر الإمكان الأكبر لنسبة النجاح P في توزيع ذو الحدين إذا سحبنا عينة عشوائية حجمها n و رمزنا


لعدد مرات النجاح بها ب X (10 درجات)

$$Z_{0.005} = 2.58, \quad Z_{0.025} = 1.96, \quad \Phi(1) = 0.8413, \quad t_{(0.025, 9)} = 2.262, \quad t_{(0.025, 8)} = 2.30622$$

مع التمنيات بالنجاح د. فاتن شيحه

111 - *المعجم - حساب - 2014/2015*
المعجم

Final Exam- Semester I - Year 2014/2015

| | | |
|-------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------|
| <p>SUBJECT: <i>Measure Theory</i> <i>(MATH 311)</i> Level-3</p> |  <p>Faculty of Science Mathematics Department</p> | <p>DATE: 29 / 12 /2014 FULL MARK: 80 ALLOWED TIME: 2Hours</p> |
|-------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------|

Answer the following questions

Question-1 (22 marks)

1. Define the algebra of sets, the outer measure on an algebra Ω , the measurable set and the measurable function
2. Prove that if Ω is an algebra of sets and $A \in \Omega$ then $A^c \in \Omega$ and any ring with this property is also algebra
3. Prove that the set of all rational numbers is countable

Question-2 (21 marks)

1. Prove that If $\mu^*(A) = 0$ then $\mu^*(A \cup B) = \mu^*(B)$
2. Prove that the family of measurable sets is an algebra
3. Prove that if $\mu^*(E) = 0$, then E is measurable

Question-3 (19 marks)

1. Prove that every continuous function is measurable
2. Prove that if f and g are measurable on a set E then so are kf, f^2 and $\min(f, g)$

Question-4 (18 marks)

1. Find the length of the set $\bigcup_{k=1}^{\infty} \left\{ x : \frac{1}{k+1} \leq x < \frac{1}{k} \right\}$
2. Show that the function
$$f(x) = \begin{cases} 1, & x \text{ is a rational number in } [0,1] \\ 0, & x \text{ is an irrational number in } [0,1] \end{cases}$$
 Is not Riemann integrable in $[0,1]$

2. calculate Lebesgue integral for the function $f(x)$
$$f(x) = \begin{cases} 1, & x \text{ is a rational number in } [a,b] \\ 2, & x \text{ is an irrational number in } [a,b] \end{cases}$$



Mansoura University, Faculty of Science, Mathematics Department
First term final exam –January, 2015 Math 313 for third year students Total Marks: 60 Time: 2 hours

يسمح باستخدام الآلة الحاسبة

Answer ALL questions. Show ALL your work. ALL questions carry equal marks.

QUESTION (1): (a) Prove: (i) $\Delta \nabla = \nabla \Delta$ (ii) $\nabla = \Delta E^{-1} = E^{-1} \Delta = 1 - E^{-1}$ (iii) $\mu = 1 + \frac{1}{4} \delta^2$.

(b) Evaluate $\Delta^4(x)_4$, if $h = 2$. (c) Express $g(x) = 3x^3 - 2x^2 + 7x - 6$ in the form $\sum_{j=0}^3 a_j(x)_{3-j}$.

(d) Use the Horner's method to evaluate $f(-1)$ and $f'(-1)$ for the polynomial $f(x)$ given by:

$$f(x) = x^5 + 6x^4 + 11x^3 + 11x^2 + 6x + 1.$$

QUESTION (2): (a) Formulate the truncation error, $E_n(x)$ of the general interpolating polynomial.

(b) Find the inverse of the matrix $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 3 & 6 \end{bmatrix}$ by using the Gauss-Jordan (G-J) method. Also find the

LU factorization of its sub-matrix $S = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix}$.

(c) Consider $B = \begin{bmatrix} p & 1 & 0 \\ q & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}$. Compute $\det(B)$ by applying the DETGTRI algorithm, then find all values of

p and q for which: (i) B is singular. (ii) B is strictly diagonally dominant. (iii) B is positive definite.

(d) The equation $x^3 - 6x - 11 = 0$ has a root between 3 and 4. By using inverse interpolation, find this root.

QUESTION (3): (a) Solve $u_n - 2u_{n-1} + u_{n-2} = 0$ given that $u_{-1} = 0$, and $u_0 = 1$.

(b) Prove that the Newton forward interpolating polynomial passing through the $(n+1)$ data points (x_i, y_i) ,

$i = 0, 1, 2, \dots, n$ such that $x_i - x_{i-1} = h = \frac{x - x_0}{s}$ is given by $P(x) = \sum_{i=0}^n \frac{(s)_i}{i!} \Delta^i y_0$.

(c) Find $y'(1.5)$ and evaluate $\int_{x=2.0}^{x=4.0} y \, dx$ by applying the Simpson's rule from the following data:

| | | | | | | |
|------|-------|-------|--------|--------|--------|--------|
| x | 1.5 | 2.0 | 2.5 | 3.0 | 3.5 | 4.0 |
| y(x) | 3.375 | 7.000 | 13.625 | 24.000 | 38.875 | 59.000 |

(d) Solve the following linear system of equations by applying the Gauss-Seidel (G-S) method.

$$-4x_1 - x_2 + 10x_3 = 24, \quad 10x_1 + 3x_2 + 2x_3 = 22, \quad -x_1 + 10x_2 + x_3 = 22.$$

انتهت الأسئلة

Kind regards

Examiner: Prof. Dr. Moawwad El-Mikkawy

Mansoura Univ.
Faculty of Science
Mathematics Dept.
Subject: Math.

3rdYear: math.

Date Jan.201

Discrete math R 347

Time:2 hours

Answer the following

1] i- Use Euclid division algorithm to find $\gcd(114,18)$ Write a program for this algorithm.


ii- State fundamental theorem of arithmetic. Use it to prove that $\log_3 20$ for the base 3 is noninteger. [27 marks]

2] i- Use Chinese remainder theorem to solve $x \equiv 1 \pmod{3}$, $x \equiv 2 \pmod{4}$.

ii- Use public key cryptography to send the word "gas".. [27 marks]

3] i- Define NP complete problem. Solve the following TSP
[*564, 3*45, 98*3, 969*]

ii- Solve $x \equiv 2 \pmod{3}$, $x \equiv 2 \pmod{6}$. [26 marks]

| | | |
|-------------------------------------------|-----------------------------------------------------------------------------------|------------------------------------------------------------------------------|
| Mansoura University Faculty of Science |  | Structured Programming Final Term Exam 1 January 2015 Time: 2 Hours |
|-------------------------------------------|-----------------------------------------------------------------------------------|------------------------------------------------------------------------------|

Question₁

- (1) Write a code segment that read four degrees from the user and display their total and minimum degree. (7 Points)
- (2) Rewrite the above code segment to work with any number of degrees specified by the user without using array. (8 Points)
- (3) Rewrite the above code segment to work with any number of degrees specified by the user using array. (8 Points)
- (4) Suppose that the values of degree are 80, 70, 90 and 60, Trace your above answer. (7 Points)

Question₂

- (1) Draw a flowchart and Write a code segment that prints the following.

(10 Points)

| | | |
|---|----|-----|
| 1 | 15 | 110 |
| 2 | 25 | 210 |
| 3 | 35 | 310 |
| 4 | 45 | 410 |
| 5 | 55 | 510 |

(2) Write a program to search for a specific value inside an array of n values accepted from the user. The program calls a method that return true if the required element exists within the array, otherwise return false. (10 Points)

Question3. Write the output of the following code segment. (10 Points)

(1)

```
int x = 2, y = 3, z = 4, m = 3, n;  
n = x-- + --z * y-- >> m;  
if (n > 1)  
    Console.WriteLine("Final");  
else  
    Console.WriteLine("Exam");
```

(2)

```
int x = 2, z = 4, m = 2, n;  
n = x++ * --z - x << ++m;  
for (int indx = n; indx > 10 ; indx /= 2)  
    Console.WriteLine("Final Exam ");
```

Good Luck



Answer the following questions.

1. Write short note for each of the following:

{10 marks}

- | | |
|-------------------------|-----------------------------|
| 1.1. Atomic domain. | 1.6. Primary key. |
| 1.2. Derived attribute. | 1.7. Referential integrity. |
| 1.3. Entity set. | 1.8. Transaction. |
| 1.4. Foreign key. | 1.9. Trigger. |
| 1.5. Metadata. | 1.10. Weak entity. |

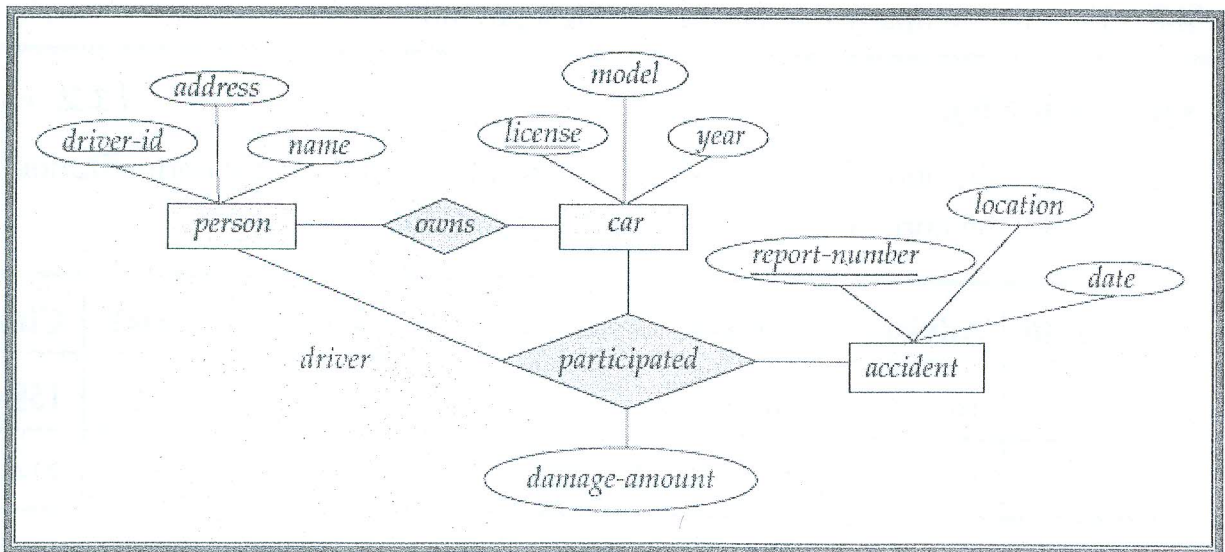
2. Question Two

{12 marks}

- 2.1. List the significant differences between a file-processing system and DBMS.
- 2.2. Define the concept of aggregation. Give two examples of where this concept is useful.
- 2.3. What is the degree of relationship set? Show example(s) using E-R model.

3. Question Three

{10 marks}



Use the E-R diagram and answer the following:

- 3.1. List the entity sets and their primary keys.
- 3.2. Design a relational database corresponding to the E-R diagram.

(Please, see next page)

4. Question Four

{16 marks}

Consider the employee database of opposite figure, where the primary keys are underlined.

| |
|-----------------------------------------------------------|
| <i>employee</i> (<u>person-name</u> , street, city) |
| <i>works</i> (<u>person-name</u> , company-name, salary) |
| <i>company</i> (<u>company-name</u> , city) |
| <i>manages</i> (<u>person-name</u> , manager-name) |

Give an expression in SQL for each of the following queries:

- 4.1. Find the names of all employees who work for First Bank Corporation.
- 4.2. Find the names and cities of residence of all employees who work for First Bank Corporation.
- 4.3. Find the names, street addresses, and cities of residence of all employees who work for First Bank Corporation and earn more than \$10,000.
- 4.4. Find all employees in the database who do not work for First Bank Corporation.
- 4.5. Find all employees in the database who earn more than each employee of Small Bank Corporation.
- 4.6. Find all employees who earn more than the average salary of all employees of their company.
- 4.7. Find the company that has the most employees.
- 4.8. Find the company that has the smallest payroll.

5. Question Five

{12 marks}

- 5.1. Define the normalization. What is the main goal of database normalization?
- 5.2. Apply the normalization forms of the un-normalized table.

| Student# | Advisor# | Advisor | Adv-Room | Class1 | Class2 | Class3 |
|----------|----------|-------------|----------|--------|--------|--------|
| 1022 | 10 | Susan Jones | 412 | 101-07 | 143-01 | 159-02 |
| 4123 | 12 | Anne Smith | 216 | 101-07 | 159-02 | 214-01 |

(End of Questions)

Good Luck

Dr. Bahaa Shabana