

المستوى: الأول

المادة: تفاضل وتكامل

كود المادة ر ١١٢



كلية العلوم - قسم الرياضيات

الزمن: ساعتين

التاريخ: ٢٠١٦/٥/١٤

الدرجة الكلية: ٨٠ درجة

البرنامج: جميع برامج المستوى الأول

أجب عن أربعة أسئلة فقط مما يلي

السؤال الأول إجباري للشعب الرياضية والفيزيائية:- (٢٠ درجة)

أ- أوجد مساحة المنطقة المحدودة بالمنحنيات $y = x^2$, $y = x + 2$
ب- أوجد كلاً من التكاملات التالية:

(٦ درجات)
(٨ درجات)

(i) $\int_{-2}^2 |x + 1| dx$

(ii) $\int \sin^2 x \cos^3 x dx$

ج- حدد مناطق التزايد والتناقص والقيم العظمى والصغرى المحلية للدالة

(٦ درجات) - $f(x) = \frac{1}{3}x^3 - x^2 - 3x + 3$

السؤال الثاني:- (٢٠ درجة)

أ- أوجد $\frac{dy}{dx}$ لكل من الدوال التالية:

(٨ درجات)

(i) $y = \tan^{-1}(5x) + (\tan 5x)^{-1}$

(ii) $y \sin x + x^3 = x e^x$

(٨ درجات)

ب- أوجد كلاً من التكاملات التالية:

(i) $\int \tan^{-1} x dx$

(ii) $\int \frac{1}{x(\ln x)^2} dx$

(٤ درجات)

ج- إدرس اتصال الدالة التالية عند $x = -3$

$$f(x) = \begin{cases} \frac{x^2 - 9}{x + 3} & , x \neq -3 \\ 5 & , x = -3 \end{cases}$$

السؤال الثالث:- (٢٠ درجة)

أ- أوجد $\frac{dy}{dx}$ لكل من الدوال التالية:

(٦ درجات)

(i) $y = (x^2 + 1)^{\cos x}$

(ii) $y = e^{\sin 3x} \sec(x^3 + 5)$

(٦ درجات)

ب- أوجد كلاً من التكاملات التالية:

(i) $\int (\tan 3x + \sec 3x)^2 dx$

(ii) $\int \frac{1}{\sqrt{4-x^2}} dx$

ج- إدرس إمكانية وجود معكوس للدالة $f(x) = \frac{x-3}{x+2}$ حيث $f: \mathbb{R} - \{-2\} \rightarrow \mathbb{R} - \{1\}$

(٨ درجات)

ثم أوجده إن وجد.

إقلب الصفحة

السؤال الرابع:- (٢٠ درجة)

أ- أوجد كلاً من التكاملات التالية:

$$(ii) \int_0^{10} \frac{x}{\sqrt{x^2 + 4}} dx$$

ب- أوجد $\frac{dy}{dx}$ لكل من الدوال التالية:

$$(ii) y = \ln(\sec x)$$

(٦ درجات)

$$(i) \int_0^1 x^2 e^x dx \quad (ii)$$

(٦ درجات)

$$(i) y = 2^{\sin^{-1} x}$$

ج- إذا كانت $f(x) = \sqrt{2-x}$ ، $g(x) = x^2 + 2x$ أوجد مجال تعريف كل منهما ثم أوجد $f \circ g$ ، $f \circ f$.
(٨ درجات)

السؤال الخامس:- (٢٠ درجة)

أ- أوجد كلاً من النهايات التالية:

$$(ii) \lim_{x \rightarrow 81} \frac{\sqrt[4]{x} - 3}{\sqrt{x} - 9}$$

(٨ درجات)

$$(i) \lim_{x \rightarrow 0^+} x \ln x$$

(٦ درجات)

ب- أوجد المشتقة الثانية للدالة $f(x) = x^2 + \frac{1}{x^2}$ عندما $x = 1$.

(٦ درجات)

$$(i) \int \frac{1}{\sqrt{x}(5 + \sqrt{x})^2} dx$$

ج- أوجد كل من التكاملات التالية:

$$(ii) \int \sec^2 x \tan^3 x dx$$

مع أطيب التمنيات
أسرة قسم الرياضيات



(Atomic weight of some elements C=12, O=16, N=14, H=1, Cu=64 and Zn=65)

Answer the following questions

1- [20marks]

a. Complete:

1) For a reversible reaction, the calculated Q (quotient) value is such that $Q < K_c$, this means that the reaction shifts to

2) Raoult's law states that : " The partial pressure of the solvent above the solution is proportional to its" "

3) If $K_a = 10^{-5}$ for acetic acid, the dissociation constant for the conjugate base is equal to.....

4) According to the kinetic theory of gases: "The kinetic energy of molecules depends on the" "

5) A chemical reaction that absorbs heat from the surroundings is said to be _____ and has a _____ ΔH at constant pressure.

b. Give a brief account on Raoul's Law.

2- a. Assign true or false for the following and comment on the answer: [20marks]

1. Osmosis is a result of passage of solute or solvent molecules through semipermeable membrane ().

2. The % ionization for weak acid = (acid concentration at initial) / (acid concentration at equilibrium) x 100 ().

3. the compressibility factor Z for an ideal gas is such that $Z = 0$ ().

4. For the reaction at equilibrium: $3Fe_{(s)} + 4H_2O_{(g)} \rightleftharpoons Fe_3O_{4(s)} + 4H_2_{(g)}$ $K_p > K_c$ ().

5. The value of ΔH° for the reaction $CH_4(g) + 3Cl_2(g) \rightarrow CHCl_3(l) + 3HCl(g)$ is -336.0 kJ. The heat (kJ) released to the surroundings when 23.0 g of HCl is formed is 71.6 KJ.

b. Deduce the relation between K_p and K_c .

3. [20 Marks]

a. Explain what colligative properties term means. .

b. Calculate the $[H^+]$ for the following solutions:

i. 0.1 M CH_3COOH ($K_a = 1.82 \times 10^{-5}$).

ii. 0.1 M CH_3COONa .

iii. Mixture from i and ii solutions

Answer the following questions

(Q1: 15 Mark, Q2: 15 Mark, Q3: 10 Mark, Q4: 20 Mark) **Full Mark: 60**

Q1:

- A) A charged wire of length L lies on z -axis, and its linear charge density varies as $\lambda = \lambda_0 z'$. Find the electrostatic field strength $\underline{E}(\underline{r})$ at a point away from the mid of the wire a distance d .
- B) Derive the 4th Maxwell's equations in case of time-dependent electromagnetics.

Q2:

- A) Solve Laplace's equation to find the electrostatic potential inside an equi-potential $[\Phi \equiv \Phi(\rho, \varphi)]$ half-cylindrical surface connected with battery of voltage V_0 and the lower plane surface connected to the ground.
- B) Define each of the following:
Polarization vector – Faraday's law – Electric dipole moment – Element of Current – Continuity equation.

Q3:

- A) Find the magnetostatic field intensity on the axis of a coil of N turns, and radius R .
- B) Prove that the net bound charge of a dielectric material vanishes.

Q4: Choose the BEST answer:

1. At point $\left(2, \frac{\pi}{4}, -3\right)$ in cylindrical coordinates, which of the following is correct
- a) $x = \sqrt{2}$ b) $\theta = 0.813\pi$ c) $r = \sqrt{13}$ d) all
2. A field \underline{F} is said to be conservative if
- a) $\underline{\nabla} \cdot \underline{F} = 0$ b) $\underline{\nabla} \times \underline{F} = 0$ c) $\int_C \underline{F} \cdot d\underline{\ell} = \rho$ d) $\underline{\nabla}(\underline{F}) = 0$
3. The continuity equation for non-steady current has the form:
- a) $\underline{\nabla} \cdot \underline{J} = 0$ b) $\underline{\nabla} \times \underline{J} = 0$ c) $\underline{\nabla} \cdot \underline{J} + \frac{\partial \rho}{\partial t} = 0$ d) $\underline{\nabla} \times \underline{J} + \frac{\partial \rho}{\partial t} = 0$
4. For isotropic, linear and homogeneous dielectric material, the relation between the polarization vector $\underline{P}(\underline{r})$ and electrostatic field intensity $\underline{E}(\underline{r})$ is given by
- a) $\underline{P}(\underline{r}) = \chi \underline{E}(\underline{r})$ b) $\underline{P}(\underline{r}) = \epsilon \chi \underline{E}(\underline{r})$ c) $\underline{P}(\underline{r}) = \epsilon_0 \chi \underline{E}(\underline{r})$ d) none
5. For any vector field \underline{A} , which of the following is correct
- a) $\underline{\nabla} \times \underline{\nabla} \times \underline{A} = 0$ b) $\underline{\nabla} \cdot \underline{\nabla} \times \underline{A} = 0$ c) $\underline{\nabla} \cdot \underline{\nabla} A_x = 0$ d) all
6. The total flux of a field \underline{A} out of a surface S surrounds a volume V , is defined by the integral
- a) $\psi = \int_V \underline{A} dv$ b) $\psi = \int_S \underline{A} \cdot \underline{\hat{n}} ds$ c) **a and b** d) none
7. Laplace's equation in electrostatics can be written for the electrostatic potential Φ as
- a) $\underline{\nabla} \Phi = 0$ b) $\nabla^2 \Phi = 0$ c) $\nabla^3 \Phi = 0$ d) none
8. Ampere's circuital law takes the form
- a) $\int_C \underline{B} \cdot d\underline{\ell} = I_{enc.}$ b) $\underline{\nabla} \cdot \underline{H}(\underline{r}) = J(\underline{r})$ c) $\int_C \underline{H} \cdot d\underline{\ell} = I_{enc.}$ d) **b and c**
9. Gauss' law in electrostatics corresponds to Maxwell's equation (write its formula after the choice)
- a) 1st b) 2nd c) 3rd d) 4th
10. The fact that "there is no single magnetic pole in nature" can be expressed mathematically as
- a) $\underline{\nabla} \times \underline{B} = 0$ b) $\underline{\nabla} \times \underline{H} = 0$ c) $\underline{\nabla} \times \underline{A} = 0$ d) $\underline{\nabla} \cdot \underline{H} = 0$