Some Preserving Subordination and Superordination of the Liu-Owa Integral Operator

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Abstract
In this paper, we obtain some subordination and superordination-preserving results of the Liu-Owa integral operator. Sandwich-type result is also obtained.

KeyWords: Analytic function; Liu-Owa operator; Hadamard product; Differential subordination; Superordination.
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Some inclusion relationships and integral-preserving properties of certain subclasses of -valent meromorphic functions associated with a family of linear operator

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Abstract

By making use of a general linear operator we introduce several new subclasses of multvalent meromorphic functions and investigate various inclusion relationships. Several interesting integral-preversing properties are also discussed.

KeyWords: Analytic function; Liu-Owa operator; Hadamard product; Differential subordination; Superordination. p-valent meromorphic functions; Hadamard product; linear operator; integral-preserving properties; inclusion relationships.

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Majorization problem for certain class of p-valently analytic function defined by generalized fractional differintegral operator

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Abstract

In this paper we investigate a majorization problem for a subclass of p-valently analytic function involving a generalized fractional differintegral operator. Some useful consequences of the main result are mentioned and relevance with some of the earlier results are also pointed out. (C) 2011 Elsevier Ltd. All rights reserved.

KeyWords: Analytic function; Differential subordination; Majorization; Fractional differintegral operator.

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ARGUMENT ESTIMATES OF CERTAIN MEROMORPHICALLY P-VALENT FUNCTIONS ASSOCIATED WITH A FAMILY OF LINEAR OPERATOR

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Abstract
Making use of linear operator we investigate some inclusion relationships and some argument properties of certain meromorphically p-valent functions. (C) 2011 Mathematical Institute Slovak Academy of Sciences.

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The Hadamard product of meromorphic univalent functions defined by using convolution

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Abstract
In this work the authors extend certain results concerning the Hadamard product for two classes related to starlike and convex univalent meromorphic functions with positive coefficients by using convolution.
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