توصيف مقرر دراسي

جامعة : المنصورة

كلية: العلوم

قسم: الرياضيات

| | | ١- بيانات المقرر |
|----------------------|--|-----------------------|
| المستوى: الرابع | اسم المقرر : Functional Analysis | كود المادة : Math 414 |
| ۲: تمارین: ۲ عملی: ۰ | عدد الوحدات الدراسية: ٣ ساعة معتمدة نظرى | التخصص : رياضيات |

| For students undertaking this course, the aims are to: | |
|---|---|
| - Familiarize the student with the basic concepts, principles and methods of Functional | |
| Analysis and its applications. Functional Analysis plays an important role in applied | |
| sciences as well as in mathematics itself. Generally speaking, Functional Analysis | |
| - Develops further the tools from Calculus and Linear Algebra to the more general | ٢- هدف المقرر: |
| setting where one has either vector spaces comprising functions or general abstract | |
| infinite-dimensional vector spaces. Problems from various application areas can then | ļ |
| be conveniently posed in this common general set up, and solved using techniques of | |
| Functional Analysis. | |
| لمقرر | ا ۳- المستهدف من تدریس ا |
| On completing this course, students will be able to: | |
| a1 – Understand the main concepts in the theories of normed spaces and inner | |
| product spaces. | أ- المعلومات و المفاهيم |
| a2 - Know the basic facts and definitions on Hilbert and Banach spaces and their duals. | : |
| a3 - State and sketch the ideas of proofs of the following theorems and principles: | |
| Holder – Minkowski – Hahn - Schwarz – Riesz representation Th. | |
| On completing this course, students will be able to: | |
| b1- construct rigorous proofs of different propositions and assertions in this context. | ب- المهارات الذهنية: |
| b2- apply basic theorems for Hilbert and Banach spaces. | |
| On completing this course, students will be able to: | |
| | ج- المهارات المهنيةالخاصة بالمقرر: |
| c1 - Extend Gram-Schmidt process to a wider class of functions. | الخاصه بالمفرر: |
| c2 - Investigate particular examples to which the theories under concern can be | |

| applied. | | | |
|--|---|---|--|
| c3 - Use lecture notes and oth | er texts to sol | ve challenging problems. | |
| On completing this course, st d1- Solve problems. d2- Work both in a team and i d3- Use Internet and Library. | | e able to: | د- المهارات العامة : |
| topology in metric span Normed spaces : define examples. subspaces - separable Bounded linear transf Finite-dimensional no The algebra of bounder spectral aspect). Inner products : examples. Orthogonality in Hilber Schmidt process. The adjoint operator - Positive operators - process of the projection Orthogonal projection | spaces – lines ormations and rmed spaces . ed linear oper ples - Schwarz ert spaces - Ries properties - scoperties – scoperties – the | d functionals. | ٤- محتوى المقرر: |
| 1- lectures.2- Tutorials.3- Quiz sheets. | | | ٥- أساليب التعليم و التعلم : |
| The same as for normal stude Science. | nts, only skele | etal disabilities are allowed in the Faculty of | ٦- أساليب التعليم و التعلم للطلب ذوى القدرات المحدودة : |
| 1- Oral Exam. | to assess | a1-a3,b1-b2,d1-d3 | |
| 2- Final Exam | to assess | a1-a3,b1-b2,c1-c3 | أ- الأساليب المستخدمة |
| 3- Mid-Term Exam | to assess | a1-a2,b1-b2,c1-c2 | |
| 1- Oral Exam | week 16 | | |
| 2- Final Exam | week 16 | | ب- التوقيت |
| 3- Mid-Term Exam | week 7 | | |

| - Mid-Term Examination 10 | |
|--|--------------------------------|
| - Final-Term Examination 80 | |
| - Oral Examination 10 | ج- توزيع الدرجات |
| - Practical Examination 0 | |
| Total 100% | |
| المراجع: | ا ٨- قائمة الكتب الدراسية و |
| - Lecture Notes. | أ- المذكرات |
| | ب- الكتب ملزمة |
| 1] W. Rudin, Functional Analysis, McGrawHill (1973). | |
| [2] F. Riesz and B. SzNagy, Functional Analysis, Dover (1990). | |
| [3] R.F. Curtain and A.J. Pritchard, Functional Analysis in Modern Applied Mathematics, Academic Press (1977). | ج- كتب مقترحة |
| [4] A.L.Brown &A.Page"Elements of Functional Analysis", London, 1970. | |
| http://www.mth.uea.ac.uk/~h720/teaching/functionalanalysis/materials/FAnotes.pdf | د- دوریات علمیة أو نشرات |
| http://www.math.nyu.edu/phd_students/vilensky/Functional_Analysis.pdf | أو نشرات |

(أ) مصفوفة المعارف والمهارات المستهدفة من المقرر الدراسي

| المحتويات للمقرر | اسبوع الدراسة | المعارف الرئيسية | مهارات ذهنية | مهارات مهنیة | مهارات عامة |
|--|------------------|---------------------|-----------------|-----------------|----------------|
| Metric spaces : definition, examples and well-known inequalities. | 1 | a1 | b1 | | d1 |
| topology in metric spaces. | 2 | a1 | b1 | c1 | d1 |
| Normed spaces : definition and examples - convergence - Banach spaces and examples. | 3 | a1,a2 | b1 | c1 | d1,d2 |
| subspaces - separable spaces - linear hulls. | 4 | a1,a2 | b2 | c1 | d1,d2 |
| Bounded linear transformations and functionals . | 5-6 | a1,a2 | b2 | c1,c2 | d1 |
| Finite-dimensional normed spaces . | 7 | a1,a2 | b2 | c1,c2 | d1,d2 |
| The algebra of bounded linear operators (an introductory account of the spectral aspect). | 8-9 | a1,a2 | b2 | c1,c2 | d1,d2 |
| Inner products: examples - Schwarz's inequality - parallelogram law - Hilbert spaces and examples. | 10 | a1, a2 | b2 | c1,c2 | d1,d2 |
| Orthogonality in Hilbert spaces - Riesz's representation Theorem - Gram-Schmidt process . | 11 | a1,a2,a3 | b2 | c1,c2 | d2,d3 |
| The adjoint operator - properties - self-adjoint bounded linear operators. | 12 | a1,a2,a3 | b1, b2 | c2,c3 | d2,d3 |
| Positive operators - properties - the spectrum, eigenvalues and eigen vectors. | 13 | a1,a2,a3 | b1, b2 | c2,c3 | d2,d3 |
| Orthogonal projections . | 14 | a1,a2,a3 | b1, b2 | c1,c2,c3 | d1,d2,d3 |

أستاذ المادة: د. محمد سمير قاسم

رئيس مجلس القسم العلمي : ا.د. مجدى إلياس فارس